

Mobile Networks

# Module C- Part 1

## WLAN

# Performance Aspects

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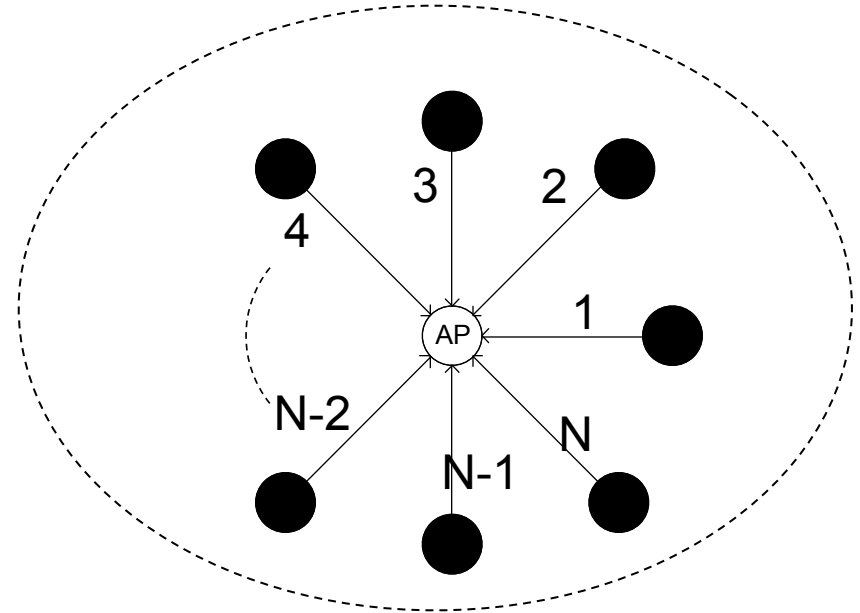
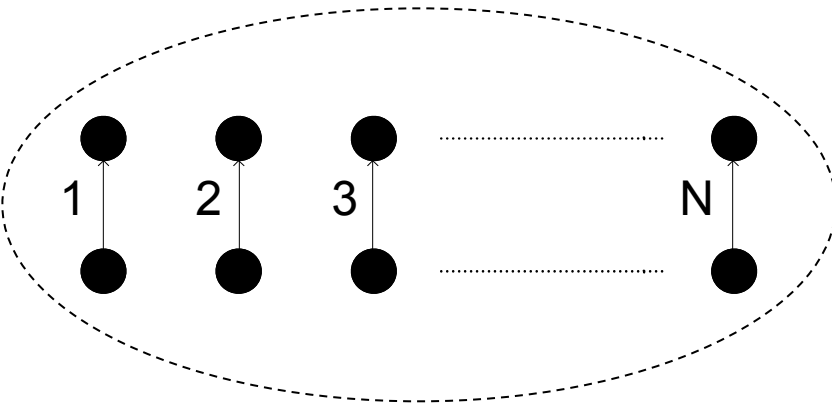
<http://mobnet.epfl.ch>

# Performance Evaluation of IEEE 802.11(DCF)

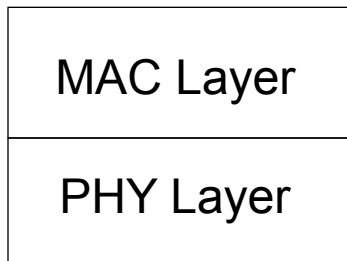
- Real Experimentations
  - HoE on IEEE 802.11b
- Analytical Models
  - Bianchi's Model
- Simulations
  - HoE on ns-2

# Bianchi's Model: Topology and Parameters

- N links with the same physical condition (single-collision domain):



We want to calculate the throughput of this network.



→  $\pi$  = Probability of Transmission



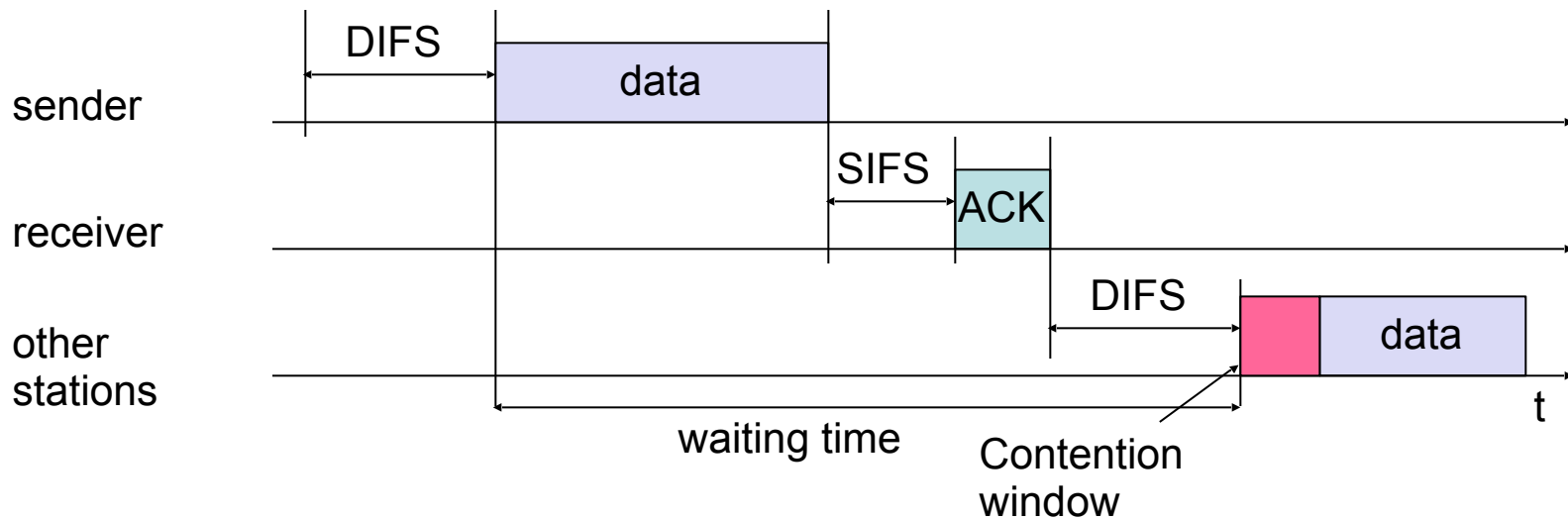
→  $p$  = Probability of Collision

= More than one transmission at the same time

$$= 1 - (1 - \pi)^{N-1}$$

# 802.11 - CSMA/CA unicast (Review)

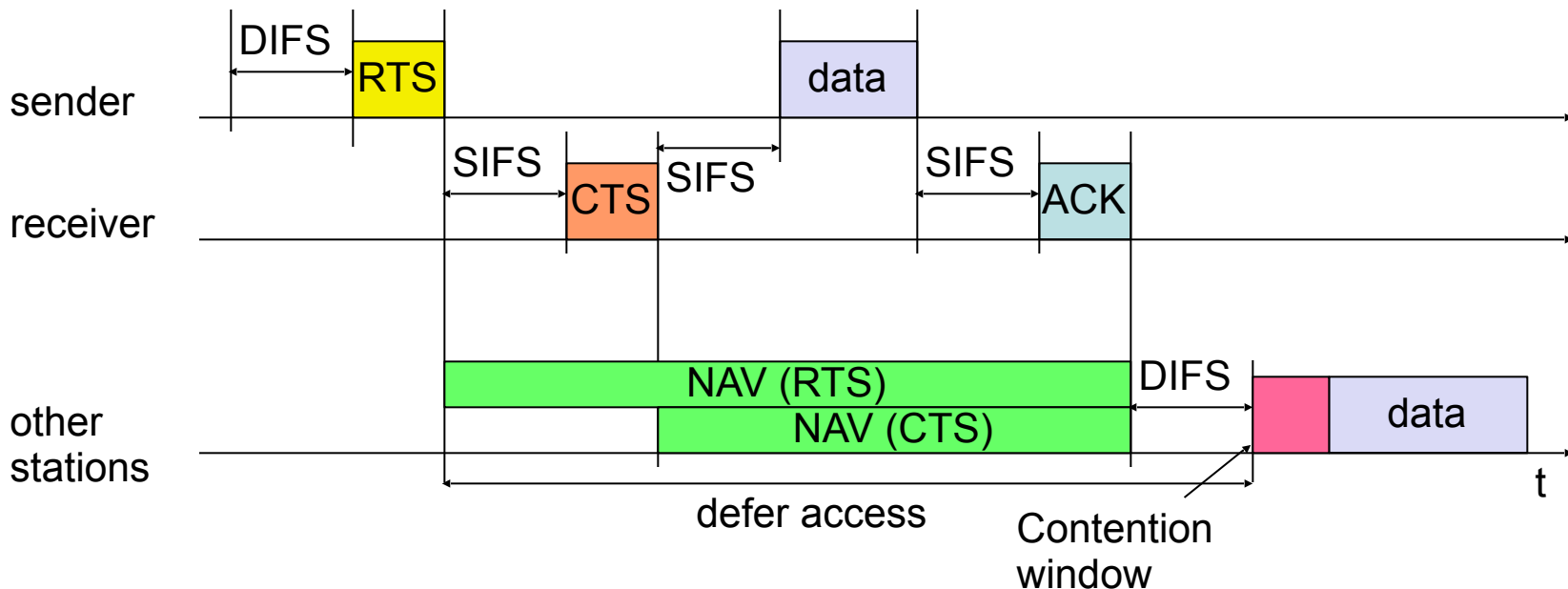
- Sending unicast packets
  - station has to wait for DIFS before sending data
  - receiver acknowledges at once (after waiting for SIFS) if the packet was received correctly (CRC)
  - automatic retransmission of data packets in case of transmission errors



The ACK is sent right at the end of SIFS (no contention)

# 802.11 – DCF with RTS/CTS (Review)

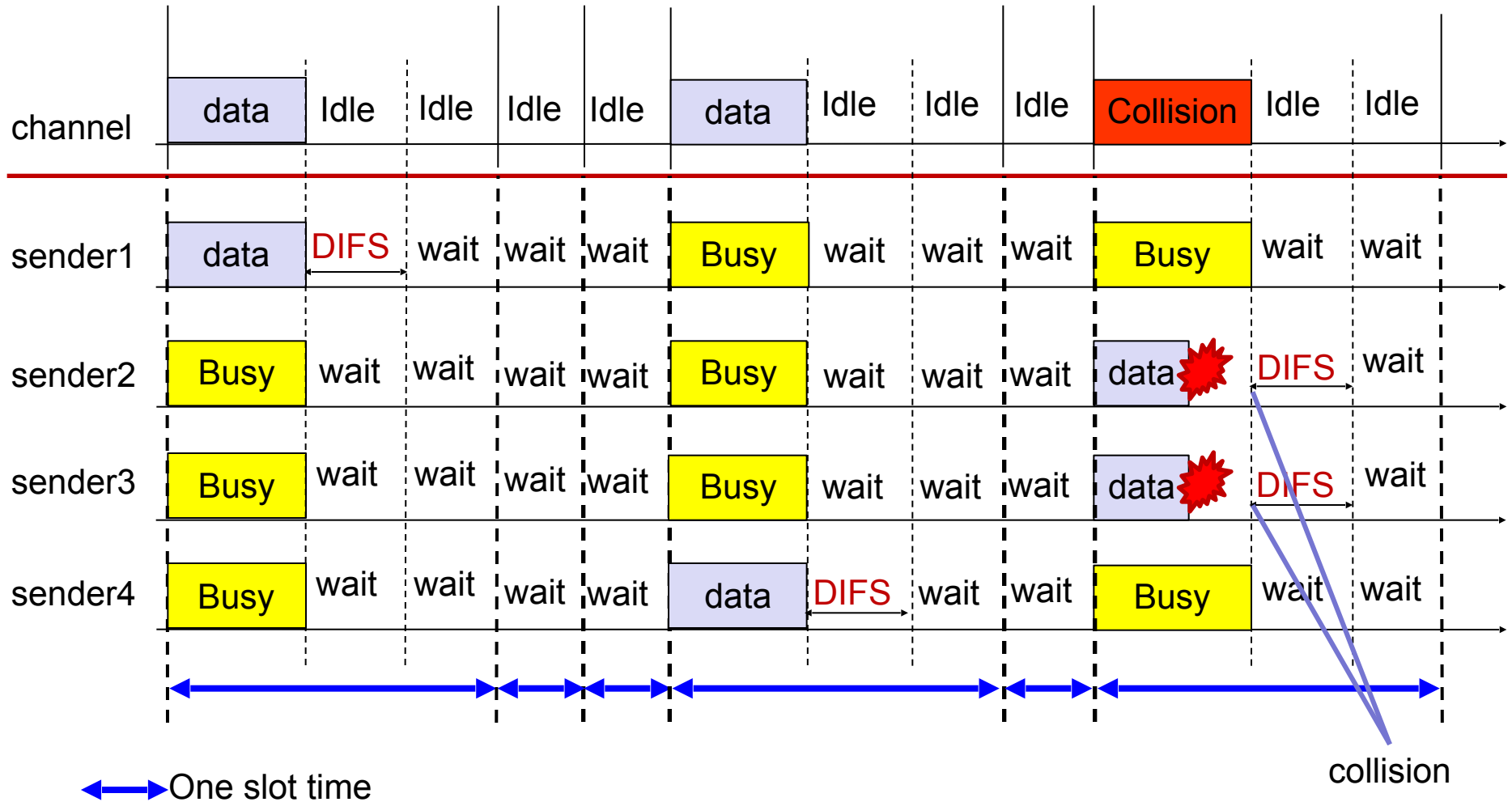
- Sending unicast packets
  - station can send RTS with reservation parameter after waiting for DIFS (reservation determines amount of time the data packet needs the medium)
  - acknowledgement via CTS after SIFS by receiver (if ready to receive)
  - sender can now send data at once, acknowledgement via ACK
  - other stations store medium reservations distributed via RTS and CTS



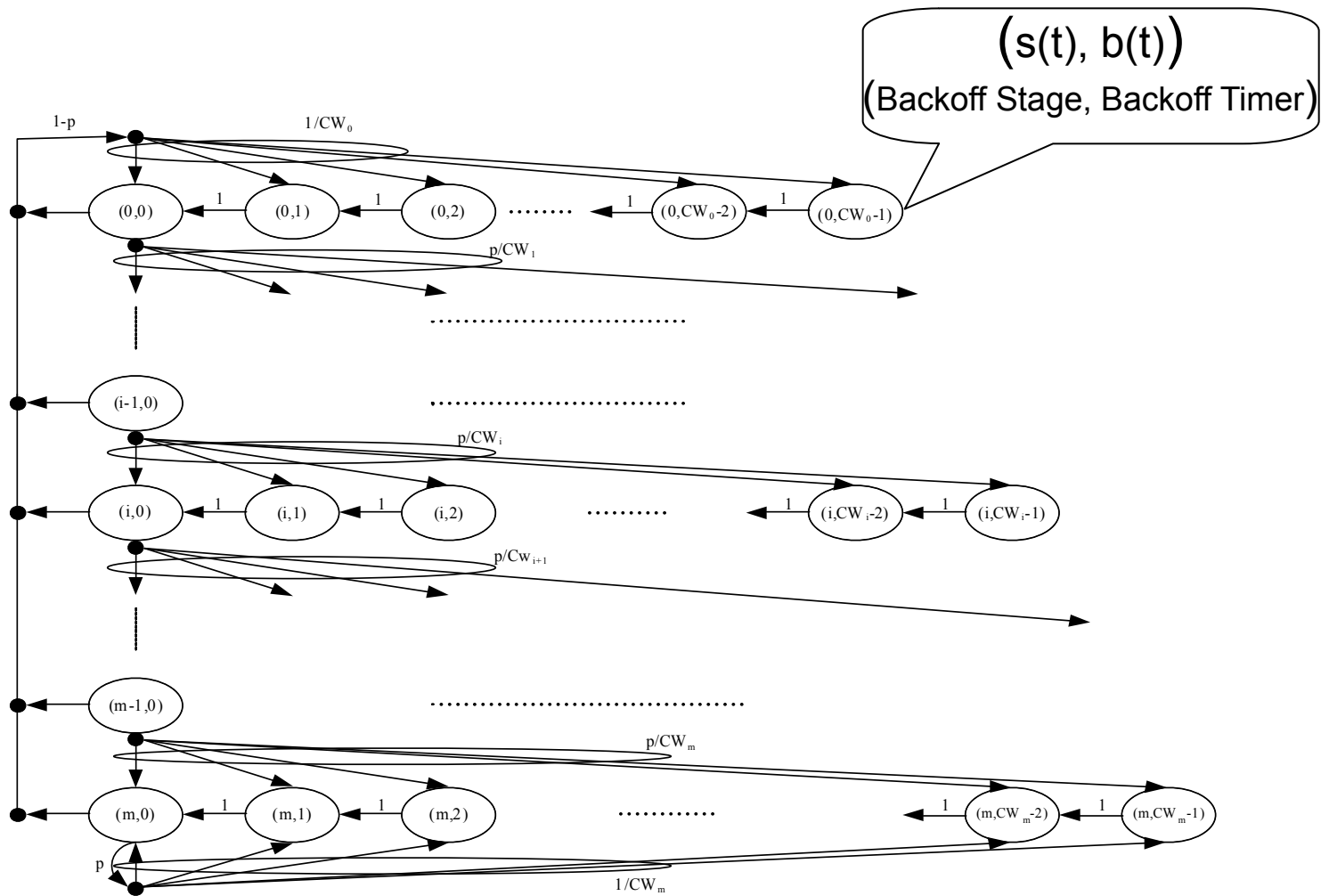
NAV: Net Allocation Vector

RTS/CTS can be present for some packets and not for other

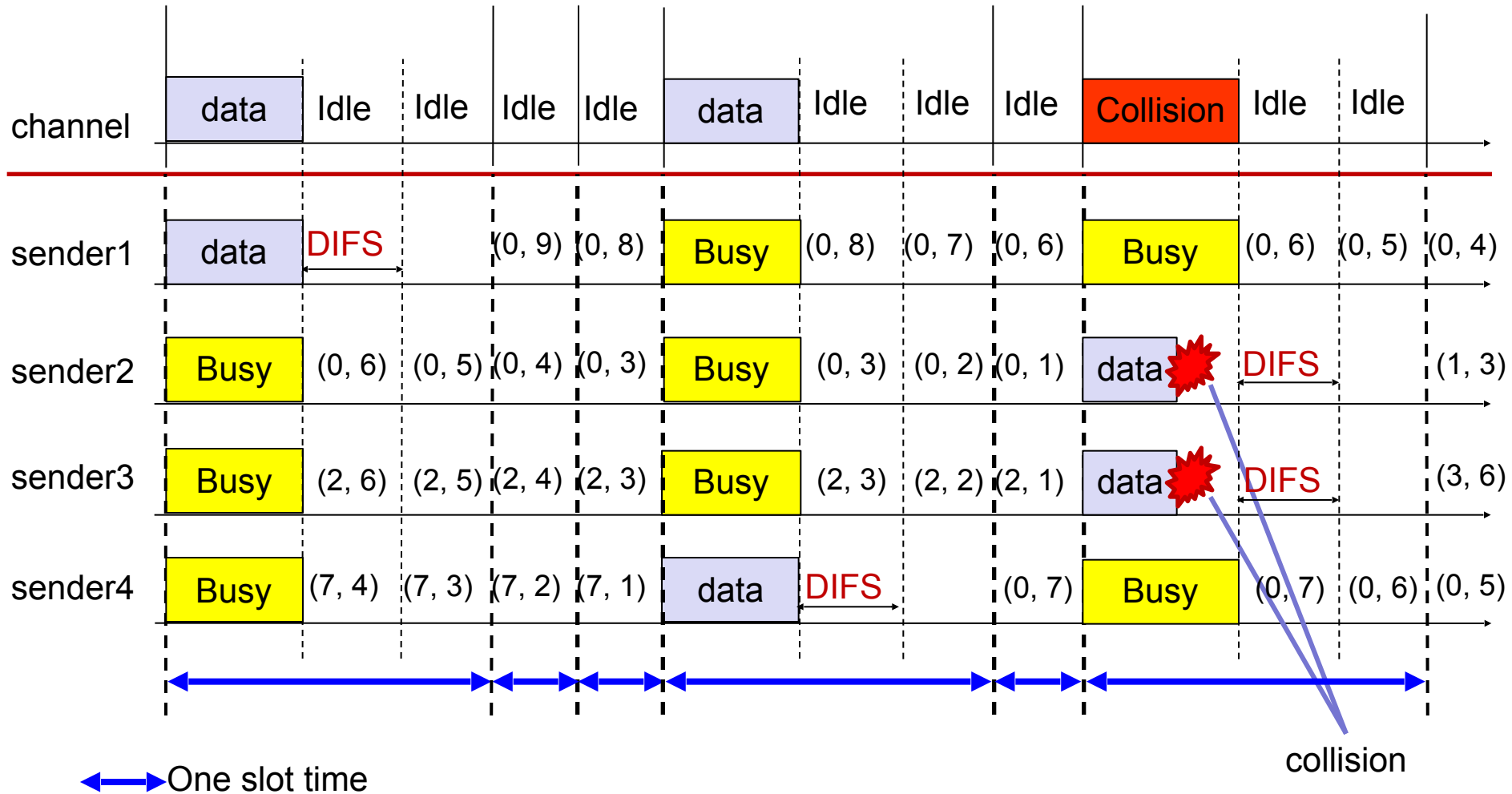
# 802.11 – Slot Time in Bianchi's Model



# Bianchi's Model: Two Dimensional Markov chain

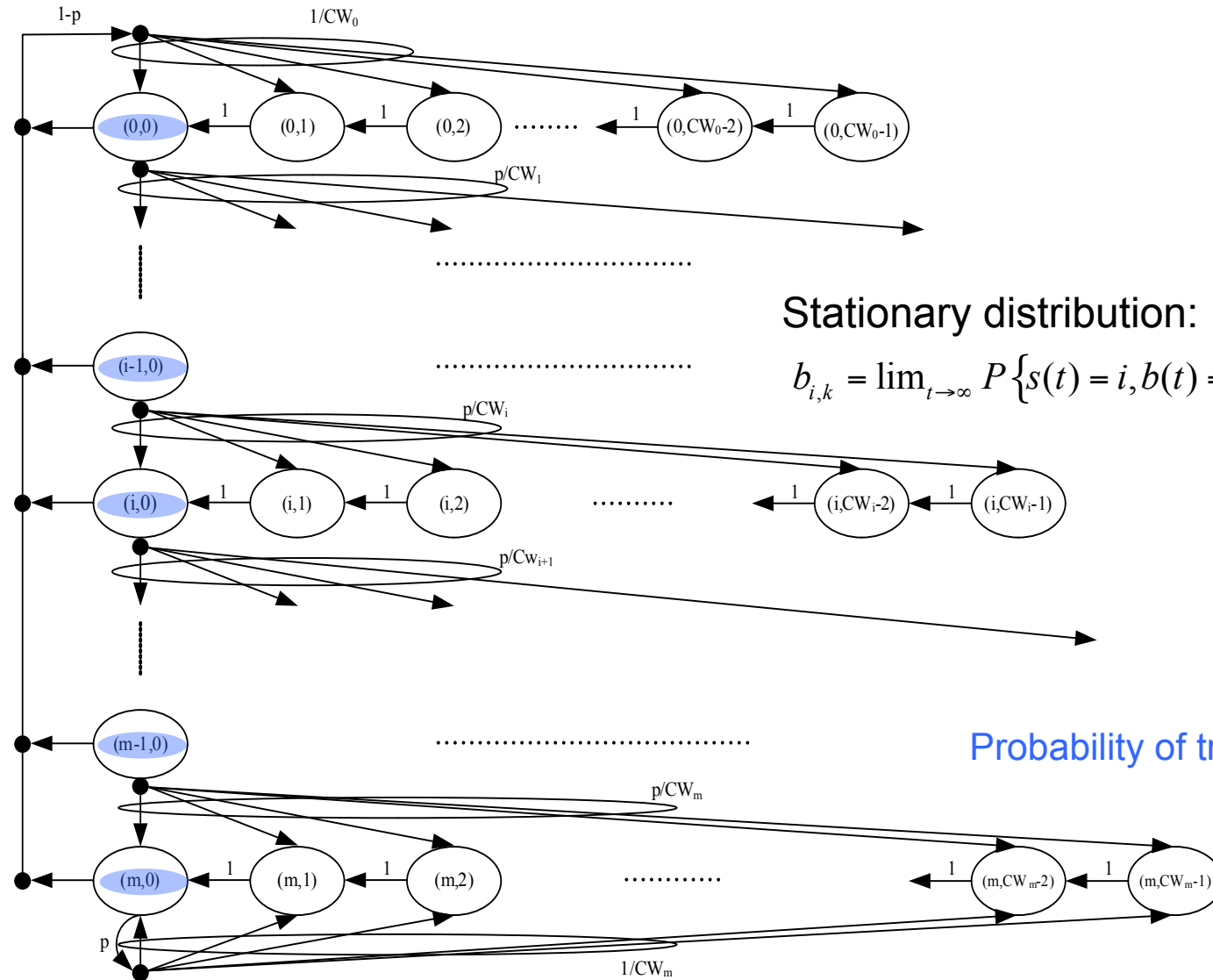


# 802.11 – Slot Time in Bianchi's Model





# Bianchi's Model: Two Dimensional Markov chain

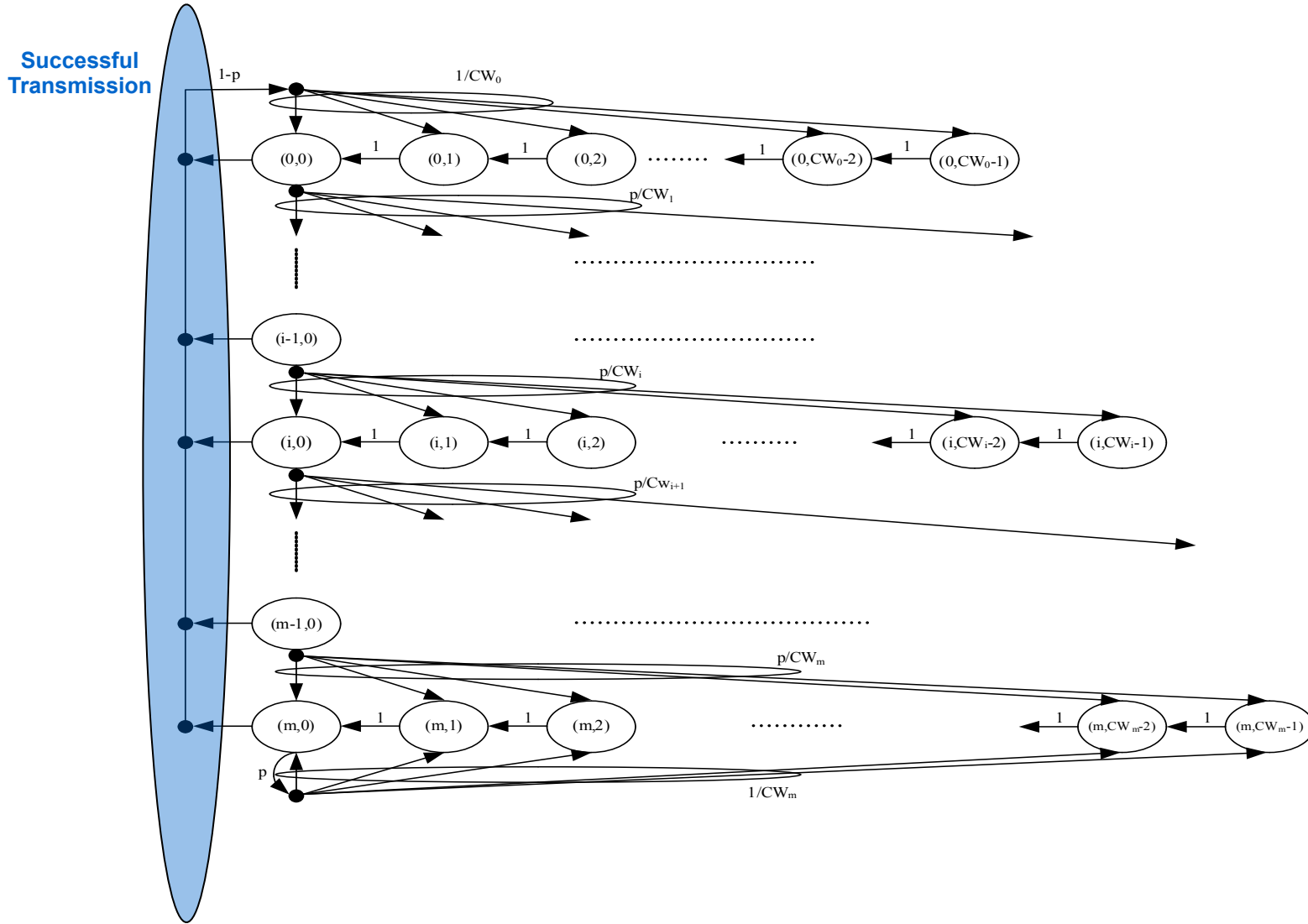


Stationary distribution:

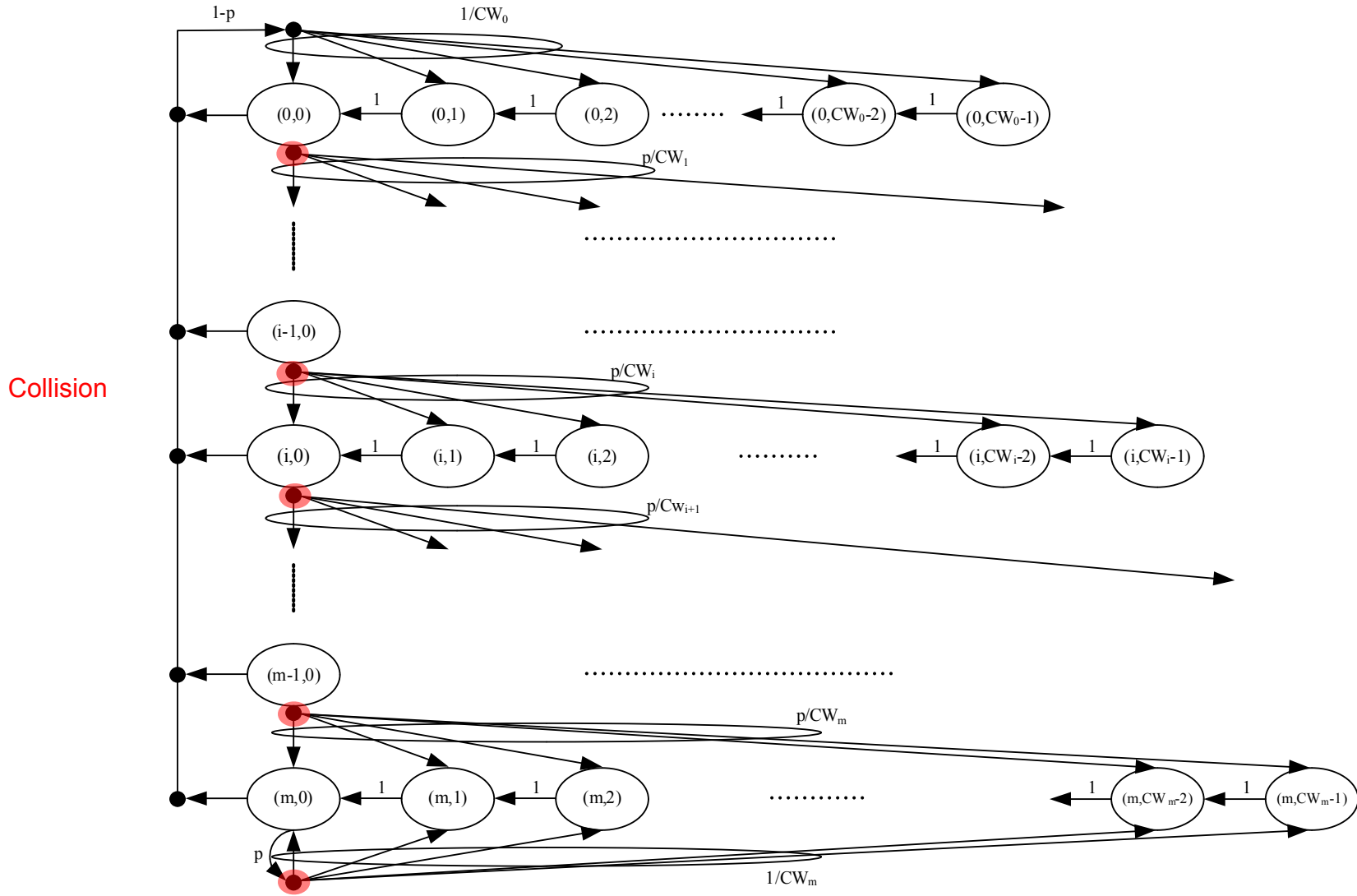
$$b_{i,k} = \lim_{t \rightarrow \infty} P \{s(t) = i, b(t) = k\}, i \in (0, m), k \in (0, CW_i - 1)$$

Probability of transmission:  $\pi = \sum_{i=0}^m b_{i,0}$

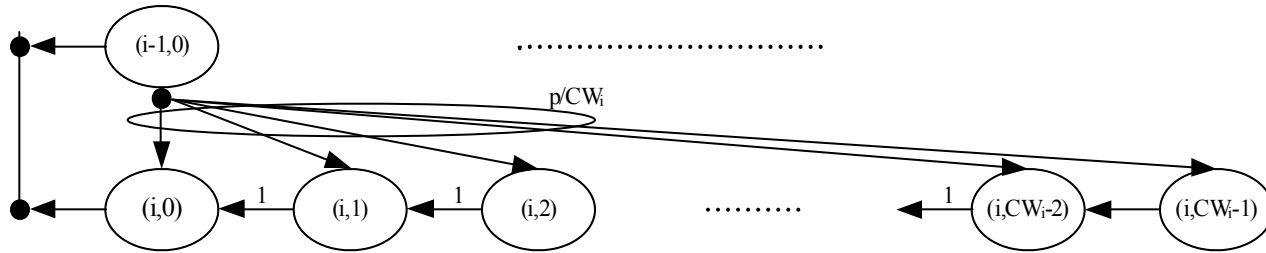
# Bianchi's Model: Two Dimensional Markov chain



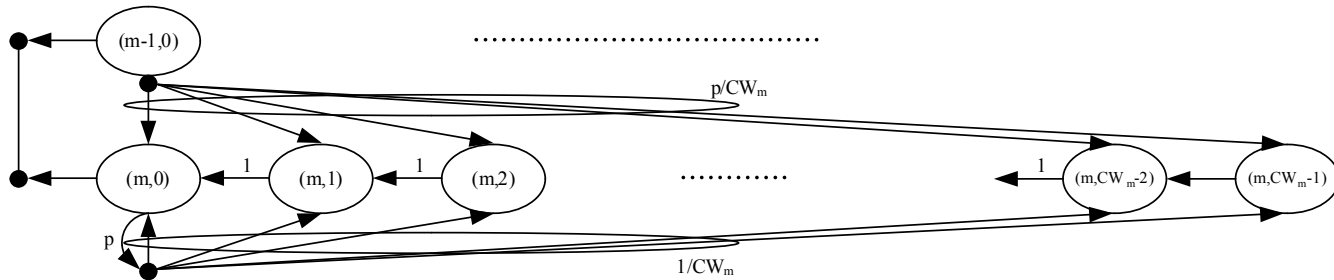
# Bianchi's Model: Two Dimensional Markov chain



# Bianchi's Model: Stationary Distribution of Chain



$$b_{i,0} = p b_{i-1,0}$$



$$b_{m,0} = p b_{m-1,0} + p b_{m,0}$$

# Bianchi's Model: Solution for $\rho$ and $\pi$

After some derivations  $\rightarrow$  system of two nonlinear equations with two variables  $\rho$  and  $\pi$ :

$$\begin{cases} \rho = 1 - (1 - \pi)^{N-1} \\ \pi = \frac{2}{1 + W_{min} + pW_{min} \sum_{k=0}^{m-1} (2p)^k} \end{cases}$$

$\rightarrow$  Can be solved numerically to obtain  $\rho$  and  $\pi$

# Bianchi's model: Throughput Calculation

- Throughput of node i:

$$\tau_i = \frac{E[\text{Payload Transmitted by user } i \text{ in a slot time}]}{E[\text{Duration of slot time}]} = \frac{P_s P_{tr} L}{P_s P_{tr} T_s + P_{tr} (1 - P_s) T_c + (1 - P_{tr}) T_{id}}$$

- $P_{tr}$ : Probability of at least one transmission in slot time
- $P_s$ : Probability of successful transmission during a random time slot
- $L$ : Average packet payload size
- $T_s$ : Average time to transmit a packet of size  $L$
- $T_c$ : Average time of collision
- $T_{id}$ : Duration of the idle period
- $t_{ACK}$ : ACK transmission time
- $t_H$ : Header transmission time
- $t_L$ : Payload transmission time

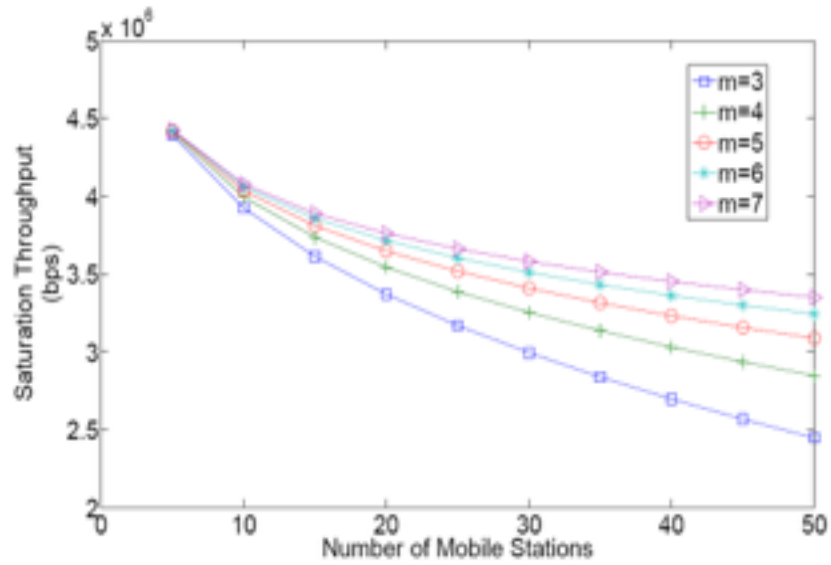
$$P_{tr} = 1 - (1 - \pi)^N$$

$$P_s = \frac{N\pi (1 - \pi)^{N-1}}{1 - (1 - \pi)^N}$$

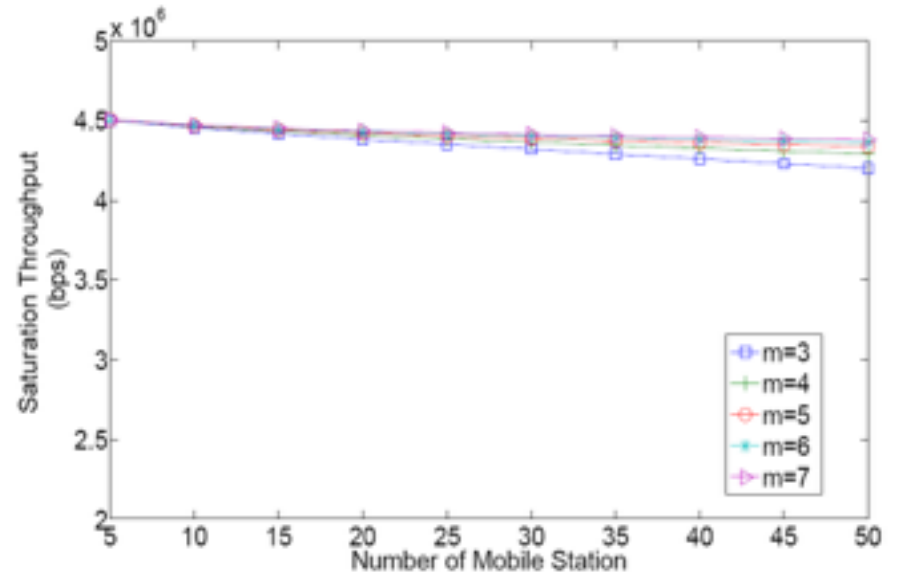
$$T_s = t_H + t_L + SIFS + \sigma + t_{ACK} + DIFS + \sigma$$

$$T_c = t_H + t_L + DIFS + \sigma$$

# Numerical Results



Basic Mode



RTS/CTS

# Conclusion

- Semi-analytical model to express the performance of IEEE 802.11 networks
- More sophisticated models have been developed since then
- Don't forget checking the related write up: «Performance Analysis of the IEEE DCF: Bianchi Model»